



Question 7 continued

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(Total 6 marks)

Q7



N 3 4 6 9 4 A 0 1 5 2 8



8. A parabola has equation $y^2 = 4ax$, $a > 0$. The point $Q(aq^2, 2aq)$ lies on the parabola.

(a) Show that an equation of the tangent to the parabola at Q is

$$yq = x + aq^2. \tag{4}$$

This tangent meets the y -axis at the point R .

(b) Find an equation of the line l which passes through R and is perpendicular to the tangent at Q . (3)

(c) Show that l passes through the focus of the parabola. (1)

(d) Find the coordinates of the point where l meets the directrix of the parabola. (2)



10.
$$\mathbf{A} = \begin{pmatrix} 3\sqrt{2} & 0 \\ 0 & 3\sqrt{2} \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \mathbf{C} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

- (a) Describe fully the transformations described by each of the matrices \mathbf{A} , \mathbf{B} and \mathbf{C} . (4)

It is given that the matrix $\mathbf{D} = \mathbf{CA}$, and that the matrix $\mathbf{E} = \mathbf{DB}$.

- (b) Find \mathbf{D} . (2)

- (c) Show that $\mathbf{E} = \begin{pmatrix} -3 & 3 \\ 3 & 3 \end{pmatrix}$. (1)

The triangle ORS has vertices at the points with coordinates $(0, 0)$, $(-15, 15)$ and $(4, 21)$. This triangle is transformed onto the triangle $OR'S'$ by the transformation described by \mathbf{E} .

- (d) Find the coordinates of the vertices of triangle $OR'S'$. (4)

- (e) Find the area of triangle $OR'S'$ and deduce the area of triangle ORS . (3)





Question 10 continued

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Question 10 continued

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Lined area for writing answers.



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